
3.1 In Class Problems

3. $f(x) = 186.5$ is a constant function, so its derivative is 0, that is, $f'(x) = 0$.

5. $f(x) = x^3 - 4x + 6 \Rightarrow f'(x) = 3x^2 - 4(1) + 0 = 3x^2 - 4$

7. $f(t) = \frac{1}{4}(t^4 + 8) \Rightarrow f'(t) = \frac{1}{4}(t^4 + 8)' = \frac{1}{4}(4t^3 + 0) = t^3$

9. $y = x^{-2/5} \Rightarrow y' = -\frac{2}{5}x^{(-2/5)-1} = -\frac{2}{5}x^{-7/5} = -\frac{2}{5x^{7/5}}$

11. $G(x) = \sqrt{x} - 2e^x = x^{1/2} - 2e^x \Rightarrow G'(x) = \frac{1}{2}x^{-1/2} - 2e^x = \frac{1}{2\sqrt{x}} - 2e^x$

13. $V(r) = \frac{4}{3}\pi r^3 \Rightarrow V'(r) = \frac{4}{3}\pi(3r^2) = 4\pi r^2$

15. $F(x) = (\frac{1}{2}x)^5 = (\frac{1}{2})^5 x^5 = \frac{1}{32}x^5 \Rightarrow F'(x) = \frac{1}{32}(5x^4) = \frac{5}{32}x^4$

17. $y = 4\pi^2 \Rightarrow y' = 0$ since $4\pi^2$ is a constant.

19. $y = \frac{x^2 + 4x + 3}{\sqrt{x}} = x^{3/2} + 4x^{1/2} + 3x^{-1/2} \Rightarrow$
 $y' = \frac{3}{2}x^{1/2} + 4(\frac{1}{2})x^{-1/2} + 3(-\frac{1}{2})x^{-3/2} = \frac{3}{2}\sqrt{x} + \frac{2}{\sqrt{x}} - \frac{3}{2x\sqrt{x}}$
[note that $x^{3/2} = x^{2/2} \cdot x^{1/2} = x\sqrt{x}$]

21. $v = t^2 - \frac{1}{\sqrt[4]{t^3}} = t^2 - t^{-3/4} \Rightarrow v' = 2t - (-\frac{3}{4})t^{-7/4} = 2t + \frac{3}{4t^{7/4}} = 2t + \frac{3}{4t\sqrt[4]{t^3}}$

23. $z = \frac{A}{y^{10}} + Be^y = Ay^{-10} + Be^y \Rightarrow z' = -10Ay^{-11} + Be^y = -\frac{10A}{y^{11}} + Be^y$

25. $y = x^4 + 2e^x \Rightarrow y' = 4x^3 + 2e^x$. At $(0, 2)$, $y' = 2$ and an equation of the tangent line is $y - 2 = 2(x - 0)$ or $y = 2x + 2$. The slope of the normal line is $-\frac{1}{2}$ (the negative reciprocal of 2) and an equation of the normal line is $y - 2 = -\frac{1}{2}(x - 0)$ or $y = -\frac{1}{2}x + 2$.

44. $f(x) = x^3 - 4x^2 + 5x \Rightarrow f'(x) = 3x^2 - 8x + 5 \Rightarrow f''(x) = 6x - 8$.
 $f''(x) > 0 \Rightarrow 6x - 8 > 0 \Rightarrow x > \frac{4}{3}$. f is concave upward when $f''(x) > 0$; that is, on $(\frac{4}{3}, \infty)$.