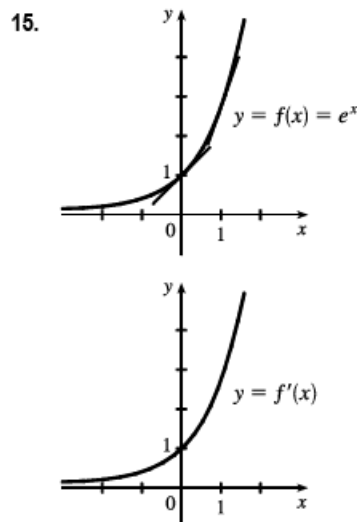


Section 2.8 Homework 1 Problems

14. See Figure 1 in Section 3.4.



The slope at 0 appears to be 1 and the slope at 1 appears to be 2.7. As x decreases, the slope gets closer to 0. Since the graphs are so similar, we might guess that $f'(x) = e^x$.

$$\begin{aligned} 23. \quad g'(x) &= \lim_{h \rightarrow 0} \frac{g(x+h) - g(x)}{h} = \lim_{h \rightarrow 0} \frac{\sqrt{1+2(x+h)} - \sqrt{1+2x}}{h} \left[\frac{\sqrt{1+2(x+h)} + \sqrt{1+2x}}{\sqrt{1+2(x+h)} + \sqrt{1+2x}} \right] \\ &= \lim_{h \rightarrow 0} \frac{(1+2x+2h) - (1+2x)}{h [\sqrt{1+2(x+h)} + \sqrt{1+2x}]} = \lim_{h \rightarrow 0} \frac{2}{\sqrt{1+2x+2h} + \sqrt{1+2x}} = \frac{2}{2\sqrt{1+2x}} = \frac{1}{\sqrt{1+2x}} \end{aligned}$$

Domain of $g = [-\frac{1}{2}, \infty)$, domain of $g' = (-\frac{1}{2}, \infty)$.

$$\begin{aligned} 25. \quad G'(t) &= \lim_{h \rightarrow 0} \frac{G(t+h) - G(t)}{h} = \lim_{h \rightarrow 0} \frac{\frac{4(t+h)}{(t+h)+1} - \frac{4t}{t+1}}{h} = \lim_{h \rightarrow 0} \frac{\frac{4(t+h)(t+1) - 4t(t+h+1)}{(t+h+1)(t+1)}}{h} \\ &= \lim_{h \rightarrow 0} \frac{(4t^2 + 4ht + 4t + 4h) - (4t^2 + 4ht + 4t)}{h(t+h+1)(t+1)} = \lim_{h \rightarrow 0} \frac{4h}{h(t+h+1)(t+1)} \\ &= \lim_{h \rightarrow 0} \frac{4}{(t+h+1)(t+1)} = \frac{4}{(t+1)^2} \end{aligned}$$

Domain of $G = \text{domain of } G' = (-\infty, -1) \cup (-1, \infty)$.

29. (a) $U'(t)$ is the rate at which the unemployment rate is changing with respect to time. Its units are percent per year.

(b) To find $U'(t)$, we use $\lim_{h \rightarrow 0} \frac{U(t+h) - U(t)}{h} \approx \frac{U(t+h) - U(t)}{h}$ for small values of h .

For 1993: $U'(1993) \approx \frac{U(1994) - U(1993)}{1994 - 1993} = \frac{6.1 - 6.9}{1} = -0.80$

For 1994: We estimate $U'(1994)$ by using $h = -1$ and $h = 1$, and then average the two results to obtain a final estimate.

$$h = -1 \Rightarrow U'(1994) \approx \frac{U(1993) - U(1994)}{1993 - 1994} = \frac{6.9 - 6.1}{-1} = -0.80;$$

$$h = 1 \Rightarrow U'(1994) \approx \frac{U(1995) - U(1994)}{1995 - 1994} = \frac{5.6 - 6.1}{1} = -0.50.$$

So we estimate that $U'(1994) \approx \frac{1}{2}[(-0.80) + (-0.50)] = -0.65$.

t	1993	1994	1995	1996	1997	1998	1999	2000	2001	2002
$U'(t)$	-0.80	-0.65	-0.35	-0.35	-0.45	-0.35	-0.25	0.25	0.90	1.10