

## Section 2.6 In Class Problems

3. The slope at  $D$  is the largest positive slope, followed by the positive slope at  $E$ . The slope at  $C$  is zero. The slope at  $B$  is steeper than at  $A$  (both are negative). In decreasing order, we have the slopes at:  $D, E, C, A$ , and  $B$ .

5. (a) (i) Using Definition 1,

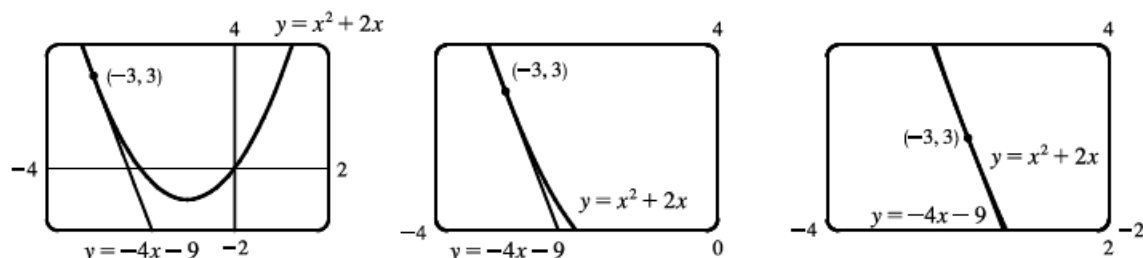
$$\begin{aligned} m &= \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} = \lim_{x \rightarrow -3} \frac{f(x) - f(-3)}{x - (-3)} = \lim_{x \rightarrow -3} \frac{(x^2 + 2x) - (3)}{x - (-3)} = \lim_{x \rightarrow -3} \frac{(x+3)(x-1)}{x+3} \\ &= \lim_{x \rightarrow -3} (x-1) = -4 \end{aligned}$$

- (ii) Using Equation 2,

$$\begin{aligned} m &= \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h} = \lim_{h \rightarrow 0} \frac{f(-3+h) - f(-3)}{h} = \lim_{h \rightarrow 0} \frac{[(-3+h)^2 + 2(-3+h)] - (3)}{h} \\ &= \lim_{h \rightarrow 0} \frac{9 - 6h + h^2 - 6 + 2h - 3}{h} = \lim_{h \rightarrow 0} \frac{h(h-4)}{h} = \lim_{h \rightarrow 0} (h-4) = -4 \end{aligned}$$

- (b) Using the point-slope form of the equation of a line, an equation of the tangent line is  $y - 3 = -4(x + 3)$ . Solving for  $y$  gives us  $y = -4x - 9$ , which is the slope-intercept form of the equation of the tangent line.

- (c)

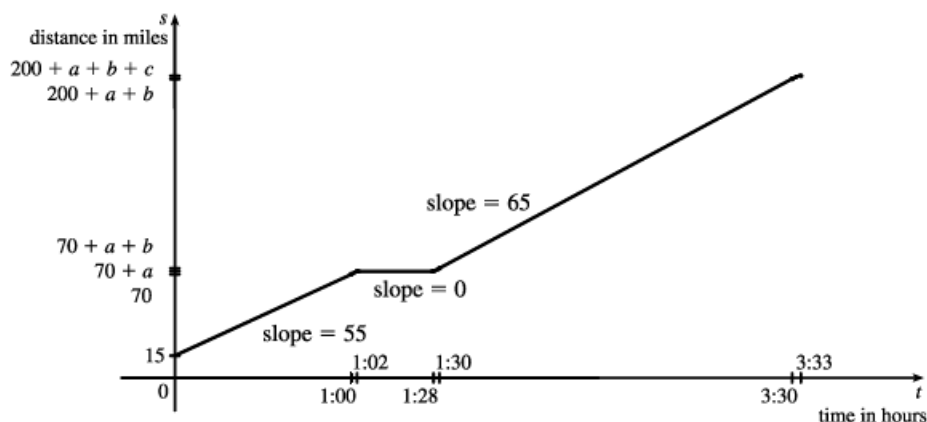


7. Using (1) with  $f(x) = \frac{x-1}{x-2}$  and  $P(3, 2)$ ,

$$m = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} = \lim_{x \rightarrow 3} \frac{\frac{x-1}{x-2} - 2}{x - 3} = \lim_{x \rightarrow 3} \frac{\frac{x-1-2(x-2)}{x-2}}{x-3} = \lim_{x \rightarrow 3} \frac{3-x}{(x-2)(x-3)} = \lim_{x \rightarrow 3} \frac{-1}{x-2} = \frac{-1}{1} = -1.$$

$$\text{Tangent line: } y - 2 = -1(x - 3) \Leftrightarrow y - 2 = -x + 3 \Leftrightarrow y = -x + 5$$

14. Let  $a$  denote the distance traveled from 1:00 to 1:02,  $b$  from 1:28 to 1:30, and  $c$  from 3:30 to 3:33, where all the times are relative to  $t = 0$  at the beginning of the trip.



17. Let  $s(t) = 40t - 16t^2$ .

$$\begin{aligned}v(2) &= \lim_{t \rightarrow 2} \frac{s(t) - s(2)}{t - 2} = \lim_{t \rightarrow 2} \frac{(40t - 16t^2) - 16}{t - 2} = \lim_{t \rightarrow 2} \frac{-16t^2 + 40t - 16}{t - 2} = \lim_{t \rightarrow 2} \frac{-8(2t^2 - 5t + 2)}{t - 2} \\&= \lim_{t \rightarrow 2} \frac{-8(t-2)(2t-1)}{t-2} = -8 \lim_{t \rightarrow 2} (2t - 1) = -8(3) = -24\end{aligned}$$

Thus, the instantaneous velocity when  $t = 2$  is  $-24$  ft/s.